

Index

This index is arranged strictly in alphabetical order according to the first significant word. Thus, 'edge connectivity' is listed under E and 'k-chromatic graph' under C.

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